

Correlated lattice fermions in a spin-dependent random potential

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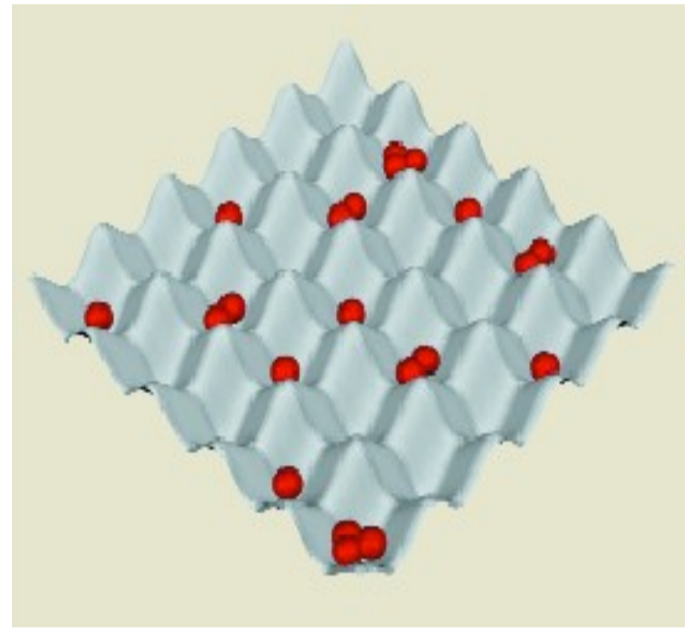
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Motivation and aims

Neutral particles in optical lattices can emulate behaviour of electrons in true materials



Interacting electrons in materials

Strongly correlated materials

Electron correlations in narrow energy bands

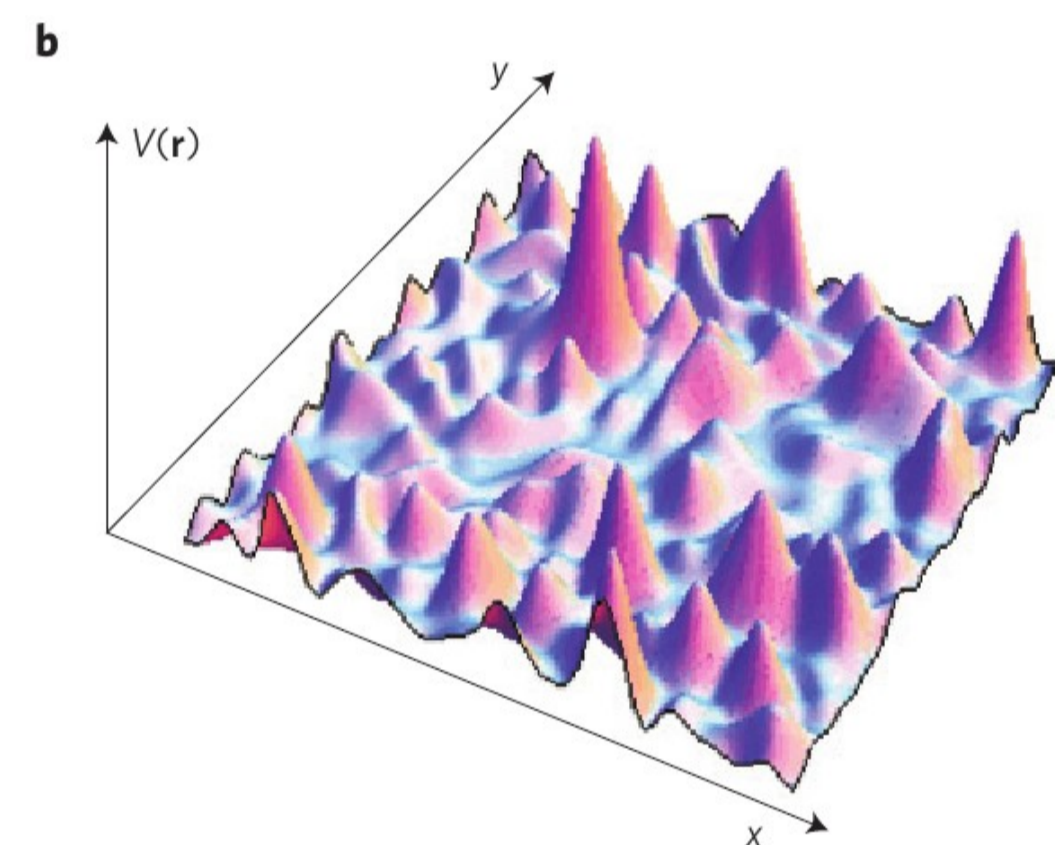
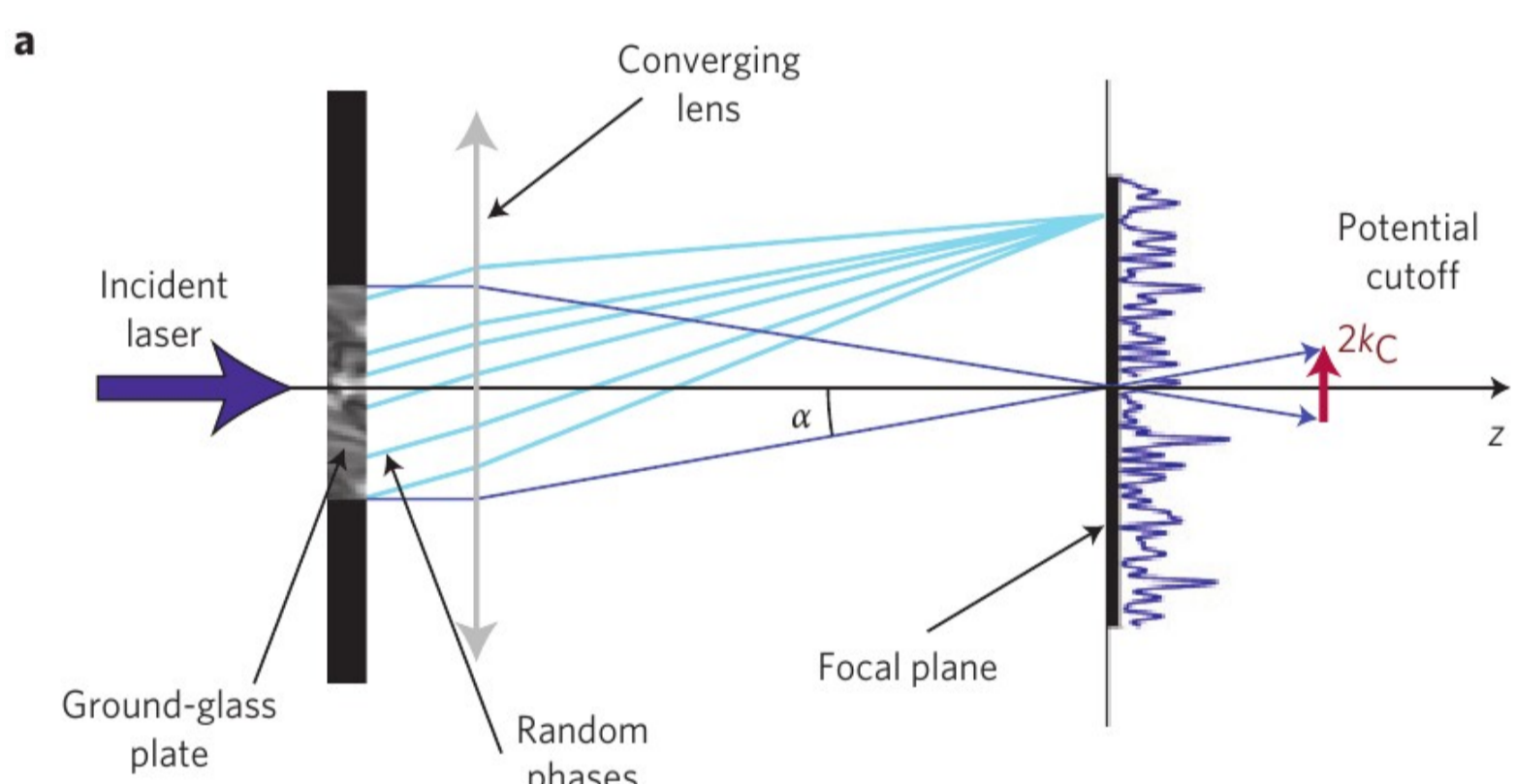
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Hubbard model (1963): that a possible approximation is to neglect all the integrals (8) apart from I . If this approximation, the validity of which is discussed in greater detail below, is made, then the Hamiltonian of (6) becomes

$$H = \sum_{i,j} \sum_{\sigma} T_{ij} c_{i\sigma}^{\dagger} c_{j\sigma} + \frac{1}{2} I \sum_{i,\sigma} n_{i\sigma} n_{i,-\sigma} - I \sum_{i,\sigma} v_{ii} n_{i\sigma} \quad (10)$$

Neutral particles in an optical lattice appeared to be a very good realization of the Hubbard model of particles in a crystal – quantum simulation of the Hubbard model.

Optical lattice with disorder



L. Sanchez-Palencia, M. Lewenstein, *Nature Phys.* 6, 87 (2010)

Spin-dependent lattices first proposed:

D. Jaksch, H. Briegel, J. Cirac, C. Gardiner, and P. Zoller, *Phys. Rev. Lett.* 82, 1975 (1999)

Spin-dependent lattices first implemented:

O. Mandel, M. Greiner, A. Widera, T. Rom, T. Hänsch, and I. Bloch, *Nature (London)* 425, 937 (2003)

P. Soltan-Panahi, J. Struck, P. Hauke, A. Bick, W. Plenkers, G. Meineke, C. Becker, P. Windpassinger, M. Lewenstein, and K. Sengstock, *Nat. Phys.* 7, 434 (2011)

also: D. McKay, B. DeMarco, *New J. Phys.* 12, 055013 (2010)

- disorder in lattice realized
- spin-dependent lattice realized

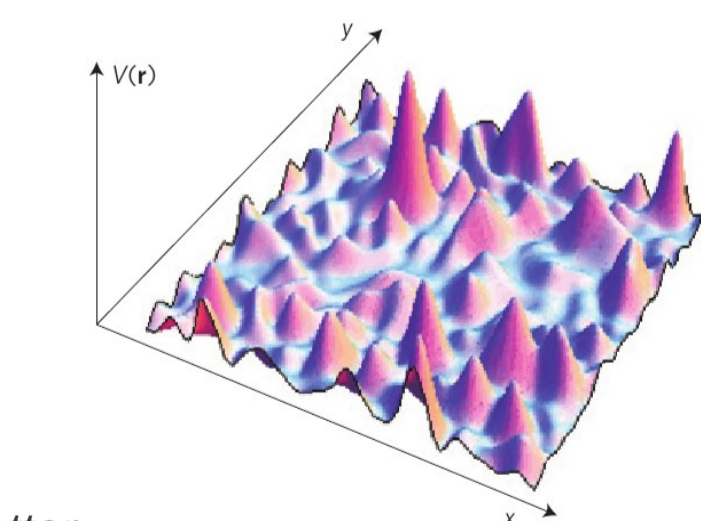
Spin-dependent disorder in optical lattice possible to realize (beyond standard solid state physics)

Comprehensive thermodynamics?

Hubbard model with spin-dependent disorder

$$H = t \sum_{(i,j)} \sum_{\sigma=\uparrow,\downarrow} \hat{c}_{i\sigma}^{\dagger} \hat{c}_{j\sigma} + \sum_i \sum_{\sigma=\uparrow,\downarrow} \epsilon_{i\sigma} \hat{n}_{i\sigma} + \sum_i U \hat{n}_{i\uparrow} \hat{n}_{i\downarrow} \quad \hat{n}_{i\sigma} \equiv \hat{c}_{i\sigma}^{\dagger} \hat{c}_{i\sigma}$$

- Disorder in the model:
- comes through diagonal terms
- quenched disorder

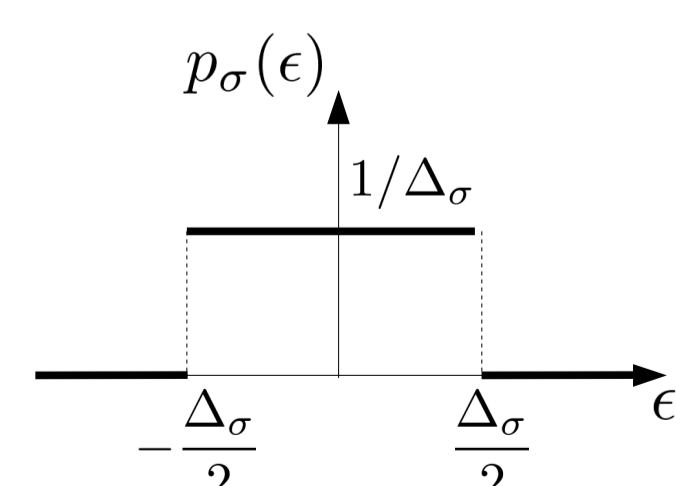


Similar model: R. Nanguneri, M. Jiang, T. Cary, G.G. Batrouni, and R.T. Scalettar, *Phys. Rev. B* 85, 134506 (2012)

but: $U < 0$, Bogolubov de Gennes mean field theory

Uncorrelated rectangular probability distribution function:

$$P(\epsilon_{1\uparrow}, \epsilon_{1\downarrow}, \dots) = \prod_i p_{\uparrow}(\epsilon_{i\uparrow}) p_{\downarrow}(\epsilon_{i\downarrow})$$



Two cases investigated here and compared:

Spin-dependent disorder:

$$p_{\uparrow}(\epsilon) \neq p_{\downarrow}(\epsilon)$$

$$\Delta_{\uparrow} = 0; \quad \Delta_{\downarrow} \equiv \Delta$$

Spin-independent disorder:

$$p_{\uparrow}(\epsilon) = p_{\downarrow}(\epsilon)$$

$$\Delta_{\uparrow} = \Delta_{\downarrow} \equiv \Delta$$

Thermodynamic properties

Magnetization: $m \equiv \lim_{N_L \rightarrow \infty} \langle \langle \sum_i \hat{n}_i \rangle \rangle_{dis} / N_L$

Double occupation: $d \equiv \lim_{N_L \rightarrow \infty} \langle \langle \sum_i \hat{n}_{i\uparrow} \hat{n}_{i\downarrow} \rangle \rangle_{dis} / N_L$

Charge susceptibility: $\chi_c = \left(\frac{\partial n}{\partial \mu} \right)_{\tau}$

Magnetic susceptibility: $\chi = \left(\frac{\partial m}{\partial h} \right)_{\tau}$

Also others: $N_{\sigma}(\mu), \dots$

Method: dynamical mean field theory

- W. Metzner, D. Vollhardt, *Phys. Rev. Lett.* 59, 121 (1987)
- A. Georges, G. Kotliar, W. Krauth, M. J. Rozenberg, *Rev. Mod. Phys.* 68, 13 (1996)
- M. Ulmke, V. Janis, D. Vollhardt, *Phys. Rev. B* 51, 10411 (1995)

$$G_{00} = \mathcal{G}_0 + \mathcal{G}_0 \Sigma \mathcal{G}_{00}$$

$$G_{00}(i\omega_n) = \int_{-\infty}^{\infty} d\epsilon \frac{D(\epsilon)}{i\omega_n - \epsilon - \Sigma(i\omega_n) + \mu}$$

$$G_{00}(\omega) = \mathcal{G}_0 + \mathcal{G}_0 \Sigma(\omega) \mathcal{G}_{00}(\omega)$$

$$G_{00}(\tau, \tau') = -\langle \langle c_{0\sigma}(\tau) c_{0\sigma}^*(\tau') \rangle \rangle_{S_{eff}[\mathcal{G}_0]_{dis}}$$

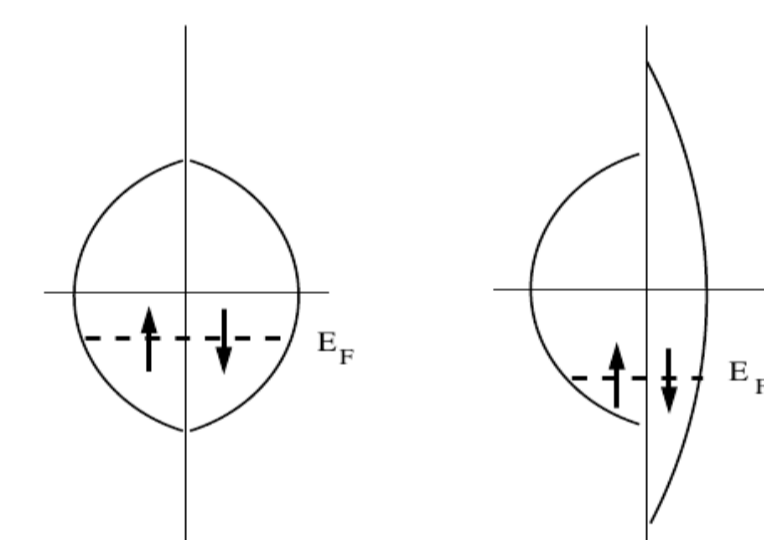
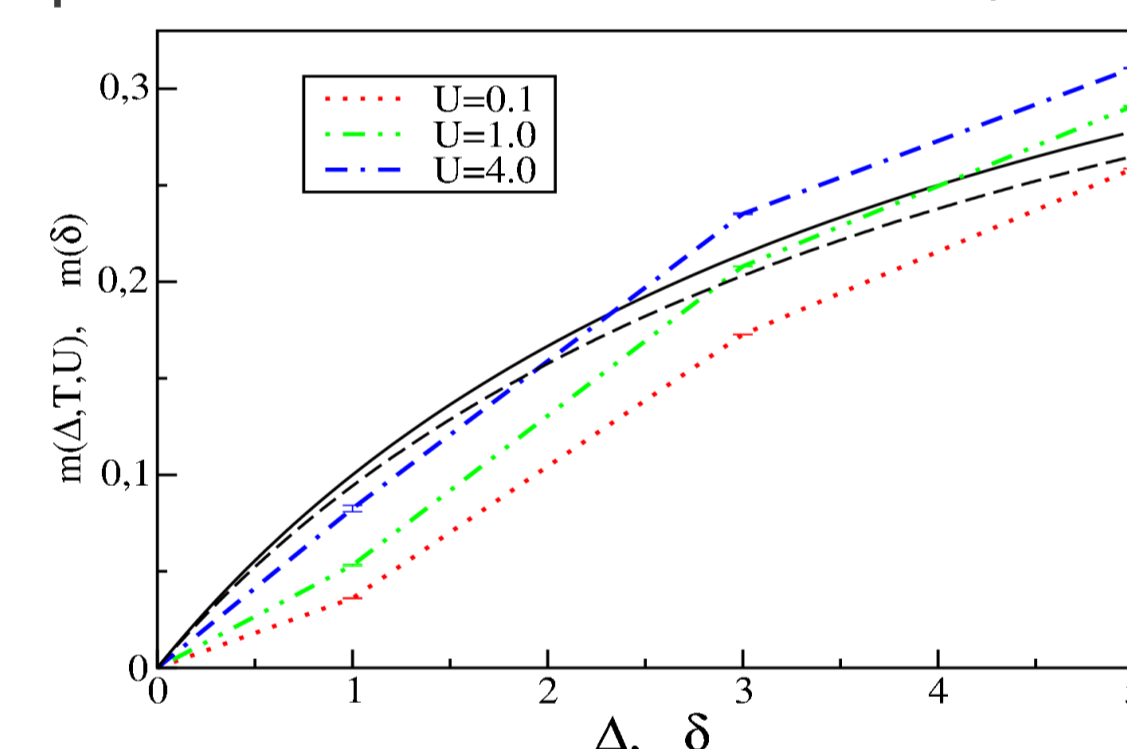
$$S_{eff} \approx \int_0^{\beta} d\tau \int_0^{\beta} d\tau' c_{0\sigma}^*(\tau) (\mathcal{G}_0^{-1}(\tau, \tau') - \epsilon) c_{0\sigma}(\tau') + \int_0^{\beta} d\tau U n_{0\downarrow}(\tau) n_{0\uparrow}(\tau)$$

Results

Magnetization

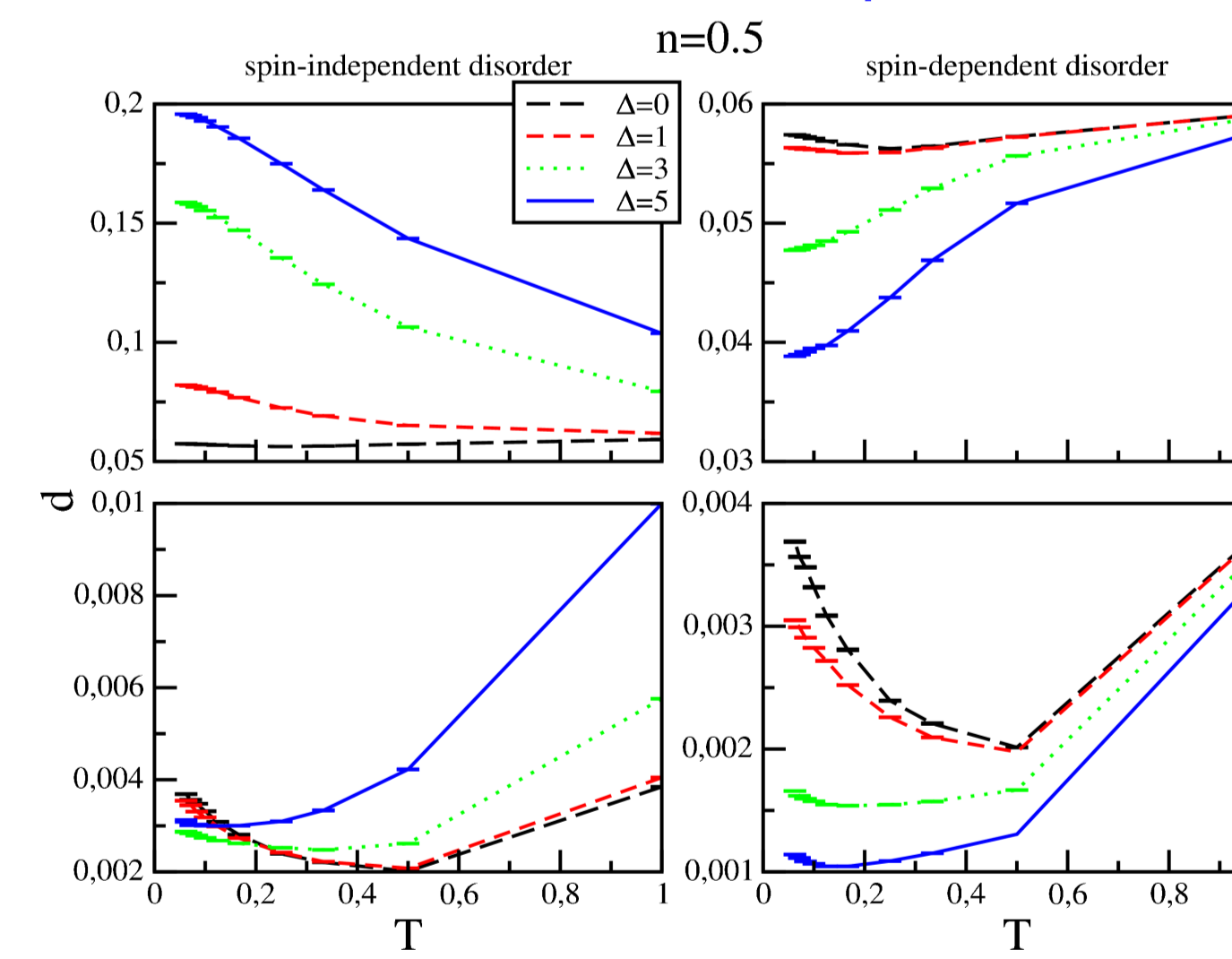
Spin-independent disorder: $m = 0$

Spin-dependent disorder: $n=0.5; T=1/16$

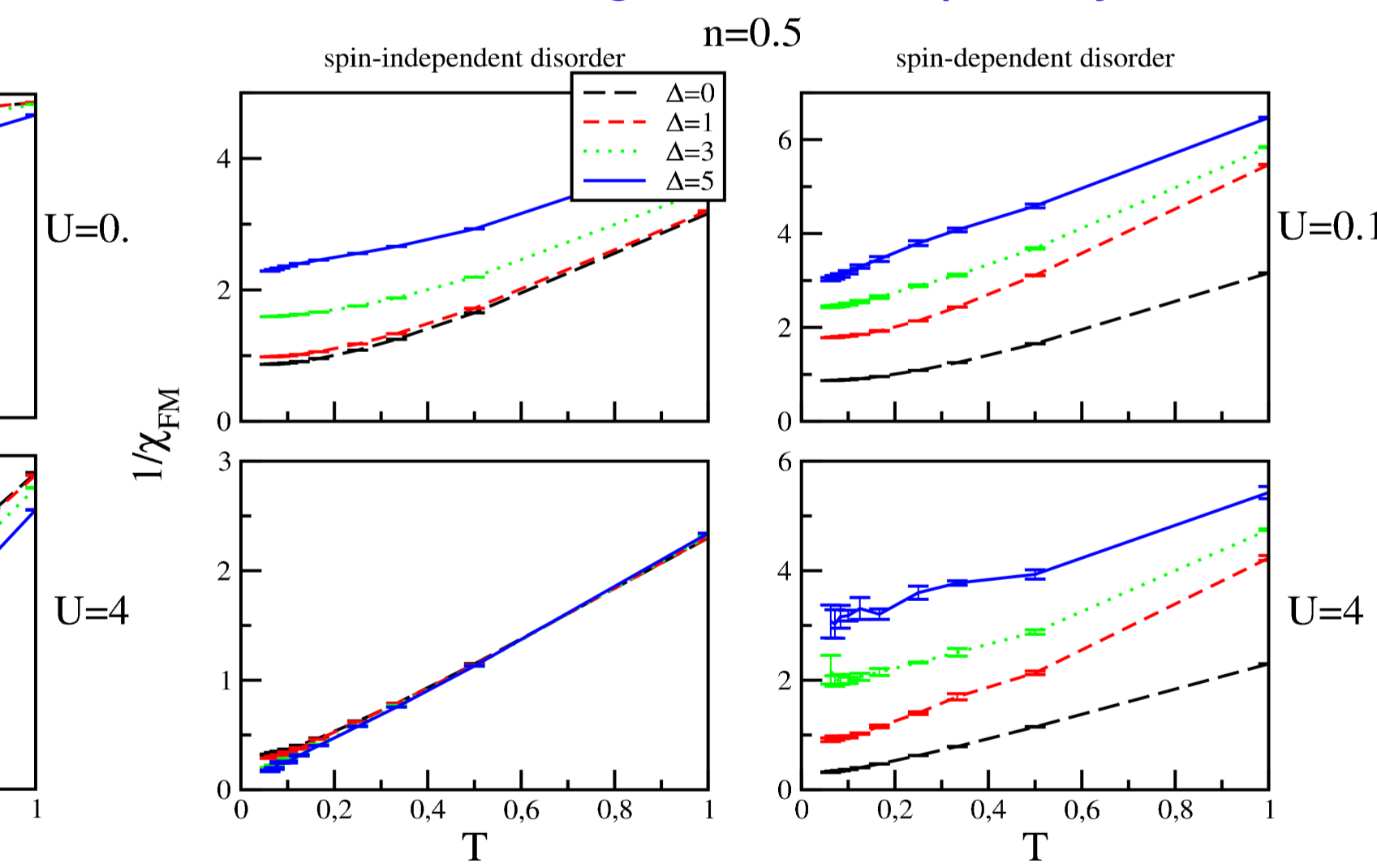


not so significant U dependence - understanding of magnetization within non-interacting system

Double occupation



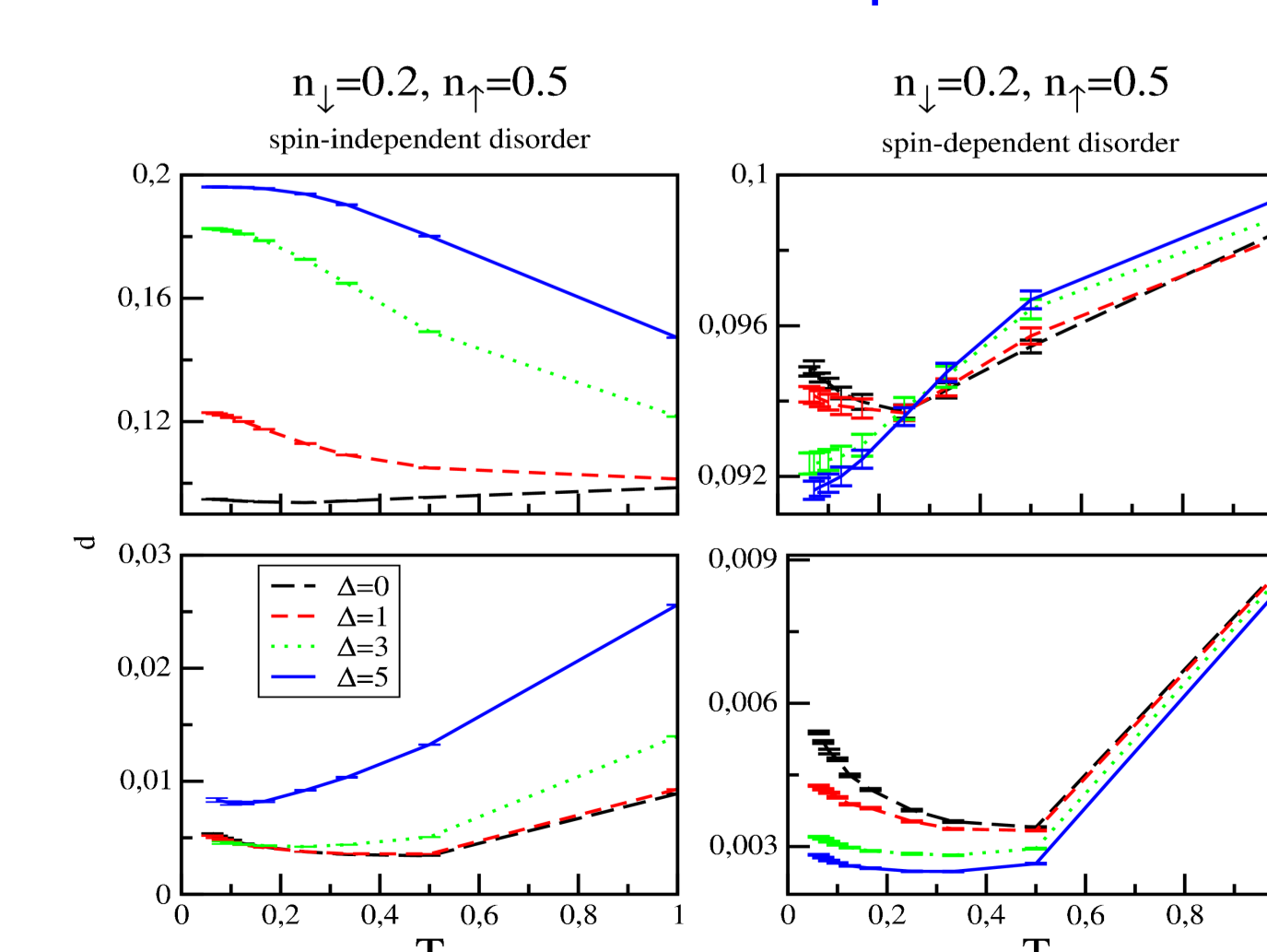
Ferromagnetic susceptibility



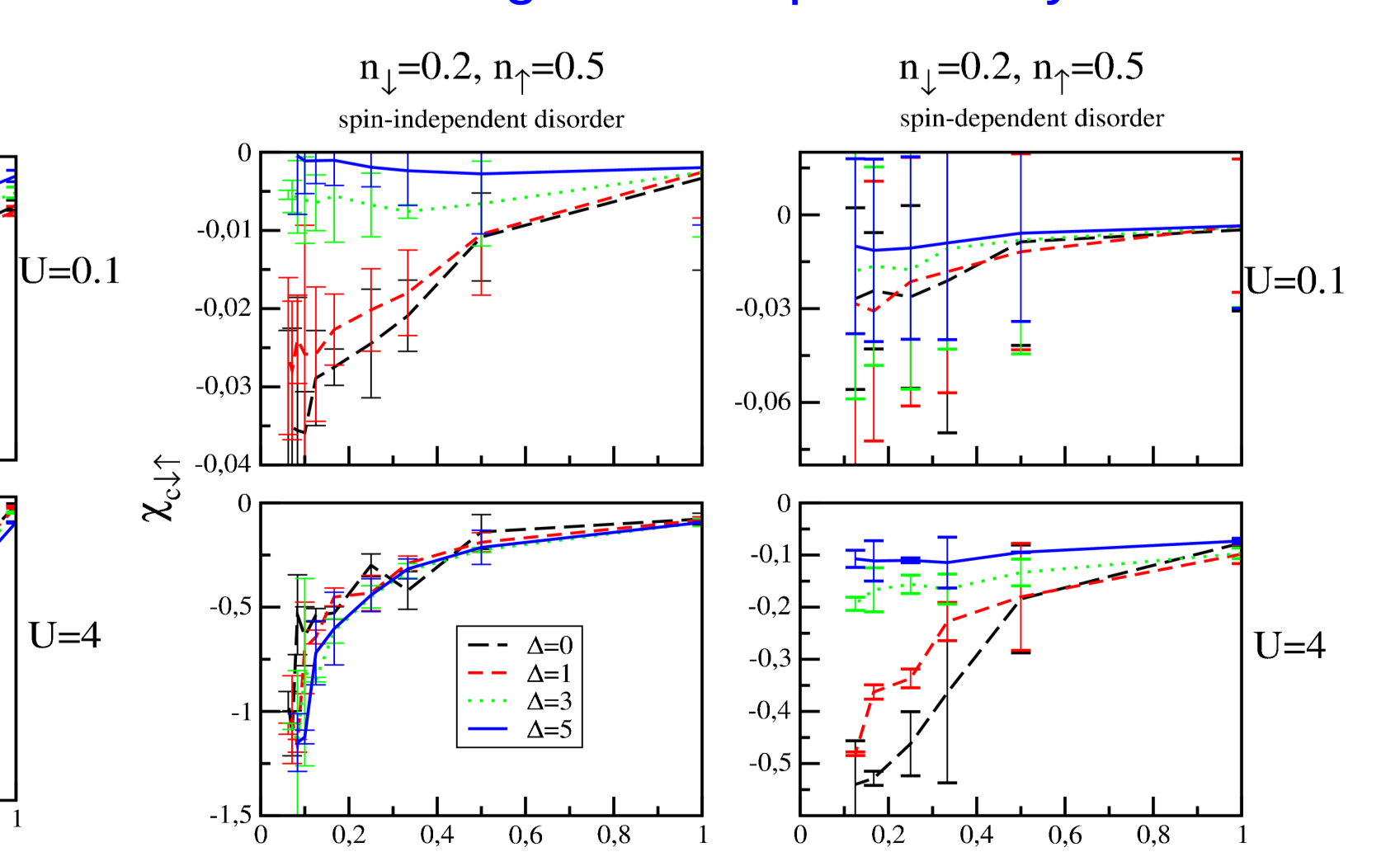
Results – spin imbalanced system

$$H = t \sum_{(i,j)} \sum_{\sigma=\uparrow,\downarrow} \hat{c}_{i\sigma}^{\dagger} \hat{c}_{j\sigma} + \sum_i \sum_{\sigma=\uparrow,\downarrow} \epsilon_{i\sigma} \hat{n}_{i\sigma} + \sum_i U \hat{n}_{i\uparrow} \hat{n}_{i\downarrow} - \mu_{\uparrow} \sum_i \hat{n}_{i\uparrow} - \mu_{\downarrow} \sum_i \hat{n}_{i\downarrow}$$

Double occupation



Off-diagonal compressibility



$$\chi_{c\sigma\sigma'} = \left(\frac{\partial n_{\sigma}(\mu_{\uparrow}, \mu_{\downarrow}, T)}{\partial \mu_{\sigma'}} \right)_{T} = \beta \langle \langle \hat{n}_{\sigma} \hat{n}_{\sigma'} \rangle \rangle_{dis} - \langle \hat{n}_{\sigma} \rangle \langle \hat{n}_{\sigma'} \rangle$$

Other thermodynamic properties in: K. M., J. Skolimowski, P. B. Chakraborty, K. Byczuk, D. Vollhardt, *New J. Phys.* 15, 045031 (2013)